

Microearthquake stress drop and attenuation from borehole DAS at Cape Modern

1/20/2026 SCEC Stress Drop Validation Workshop

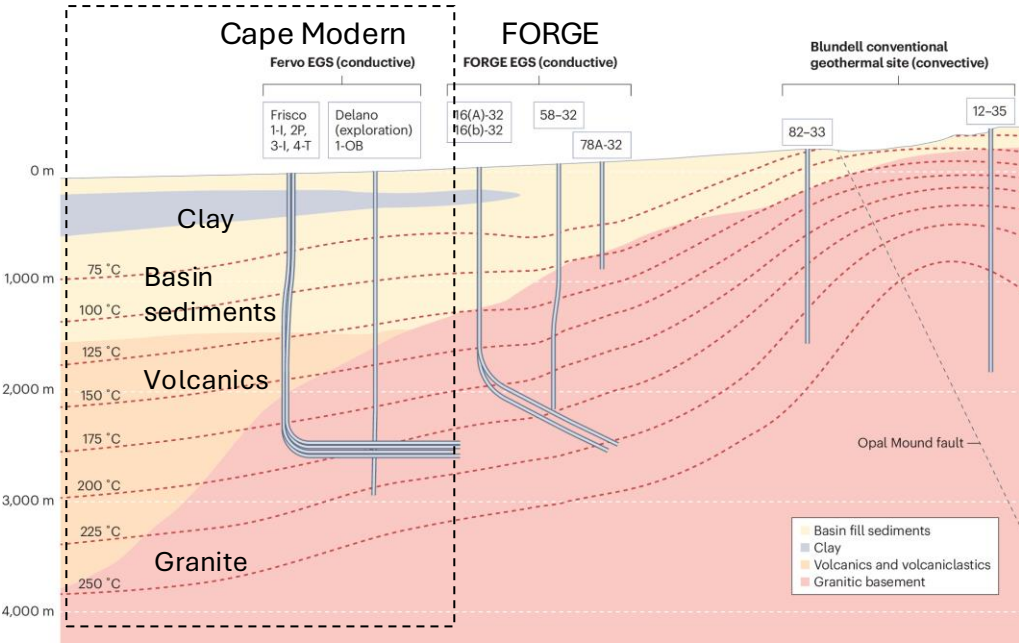
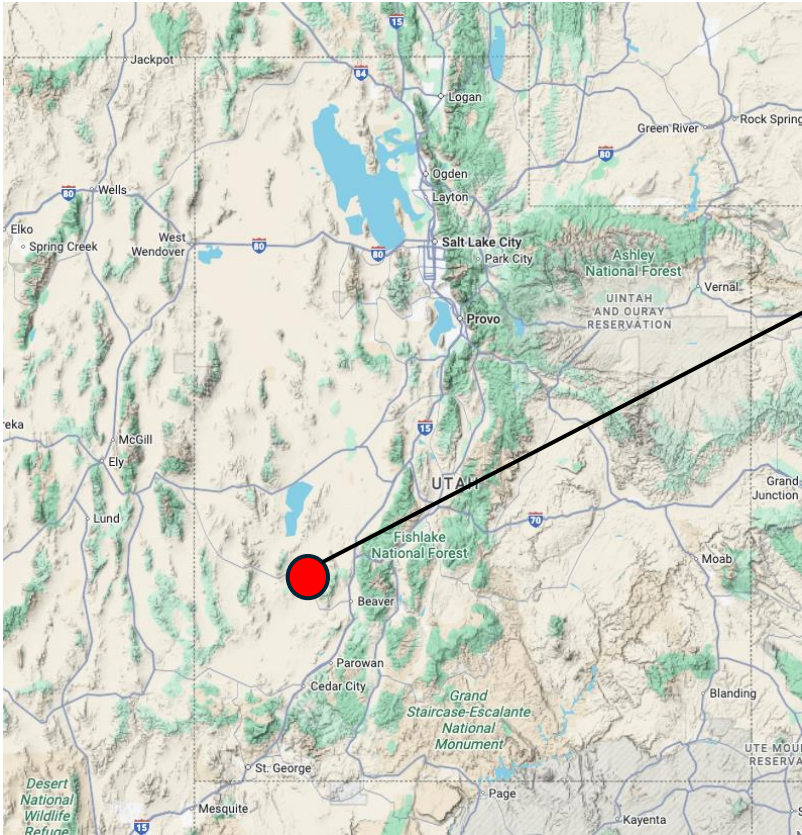
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Sireesh Dadi⁴, and Aleksei Titov⁴

LAMONT-DOHERTY EARTH OBSERVATORY¹
COLUMBIA CLIMATE SCHOOL



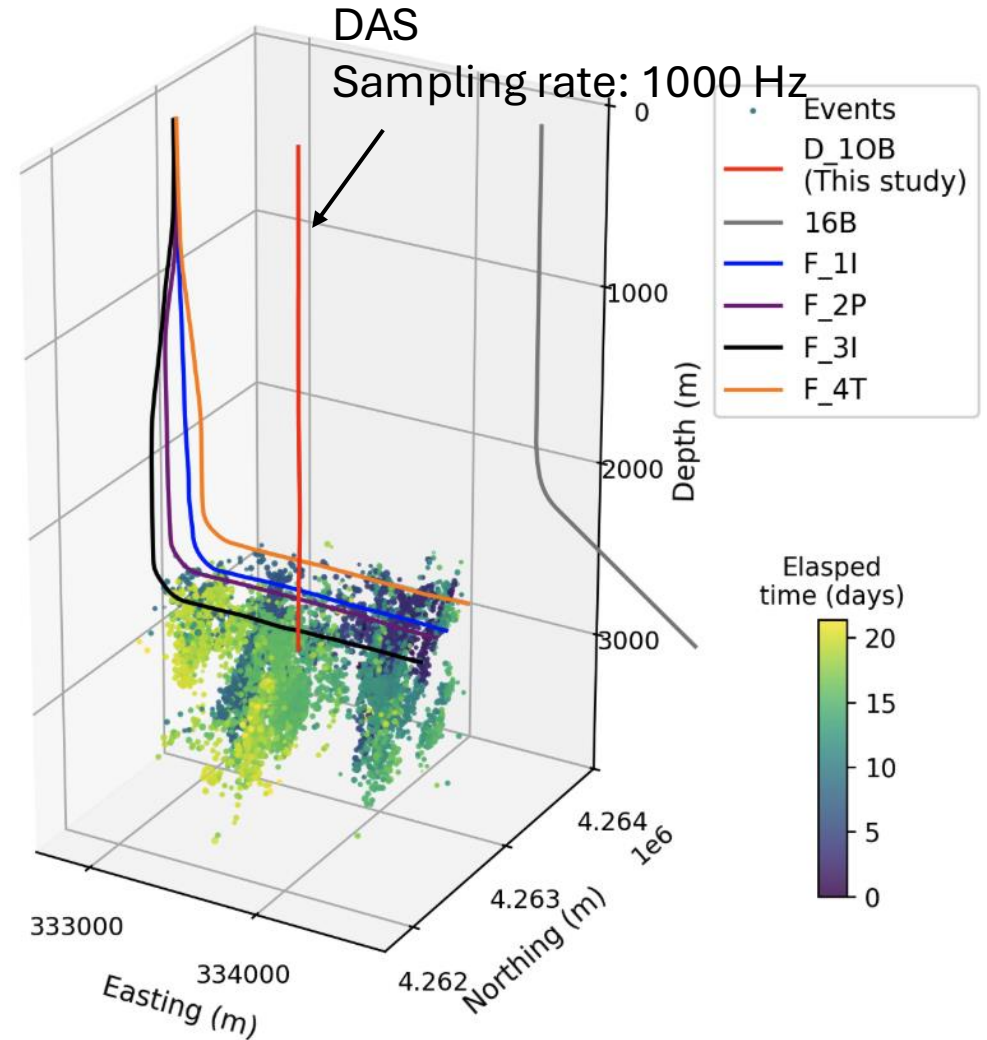
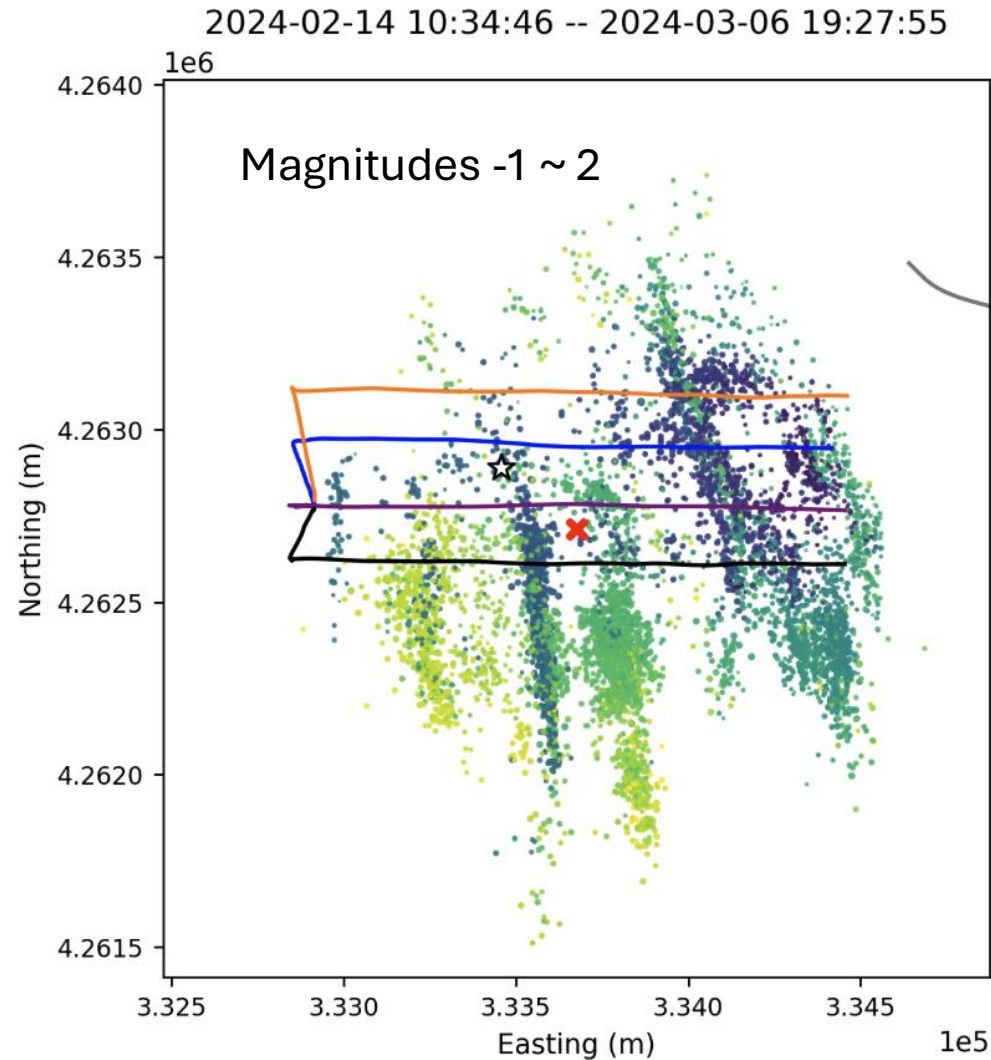
Cape Modern geothermal field in Utah

Enhanced Geothermal System (EGS)

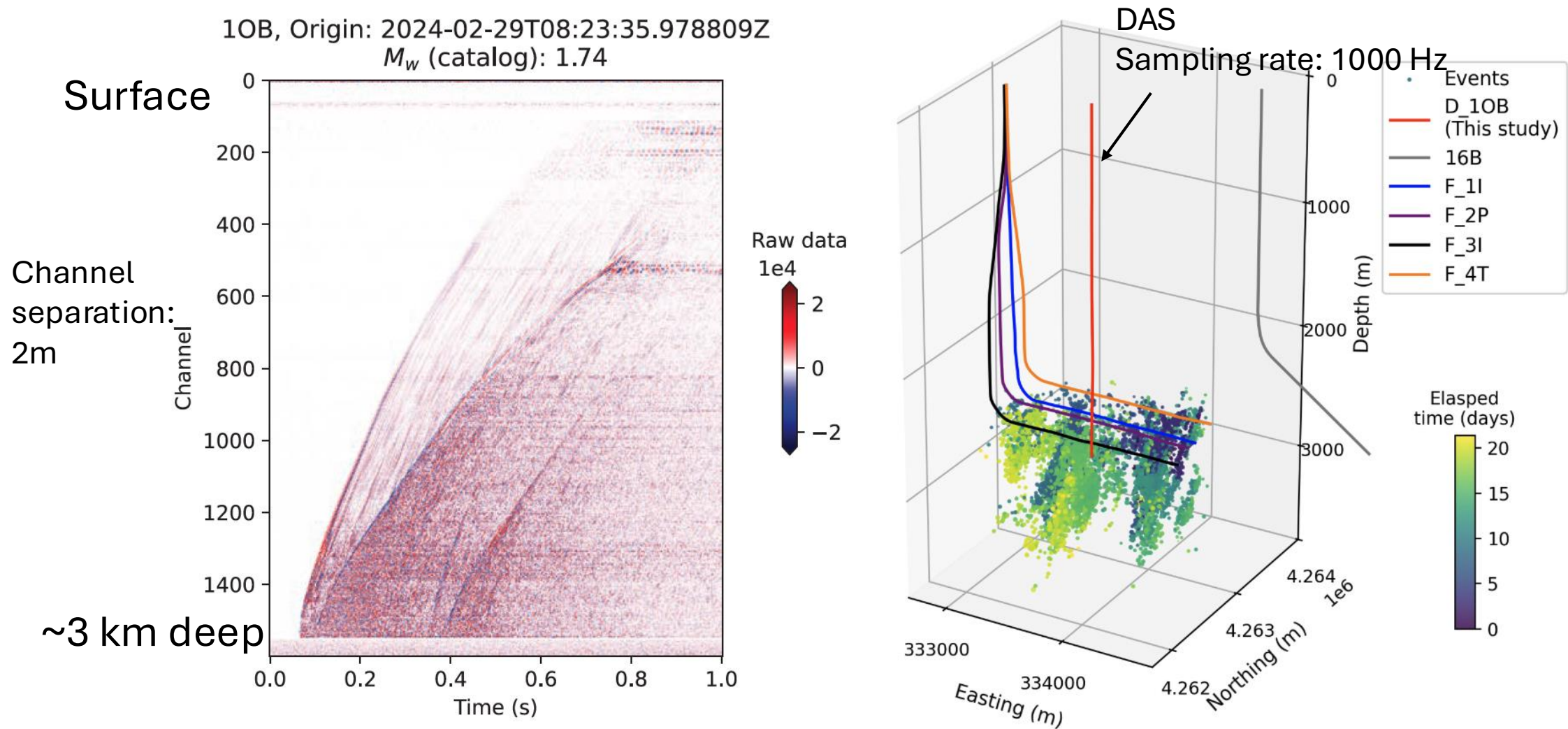


Horne et al. (2025)

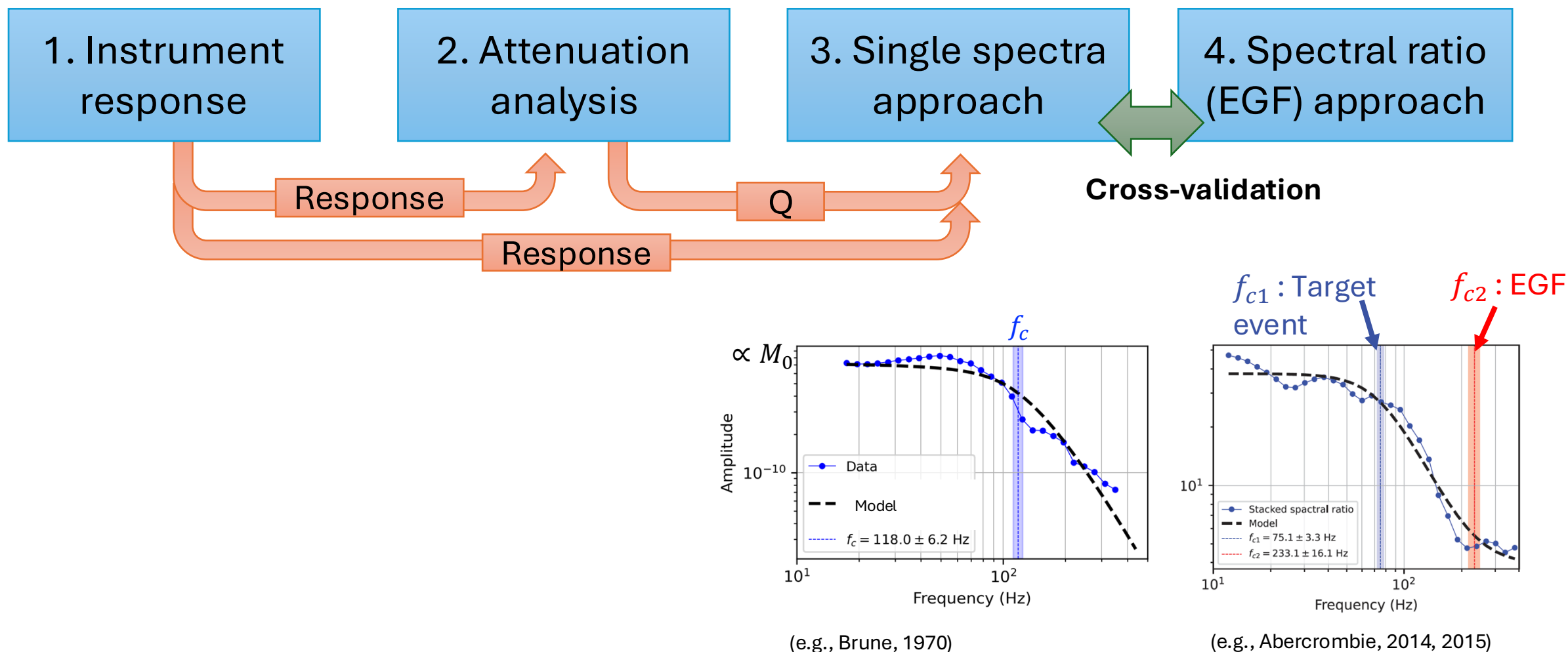
Microearthquakes induced by stimulation



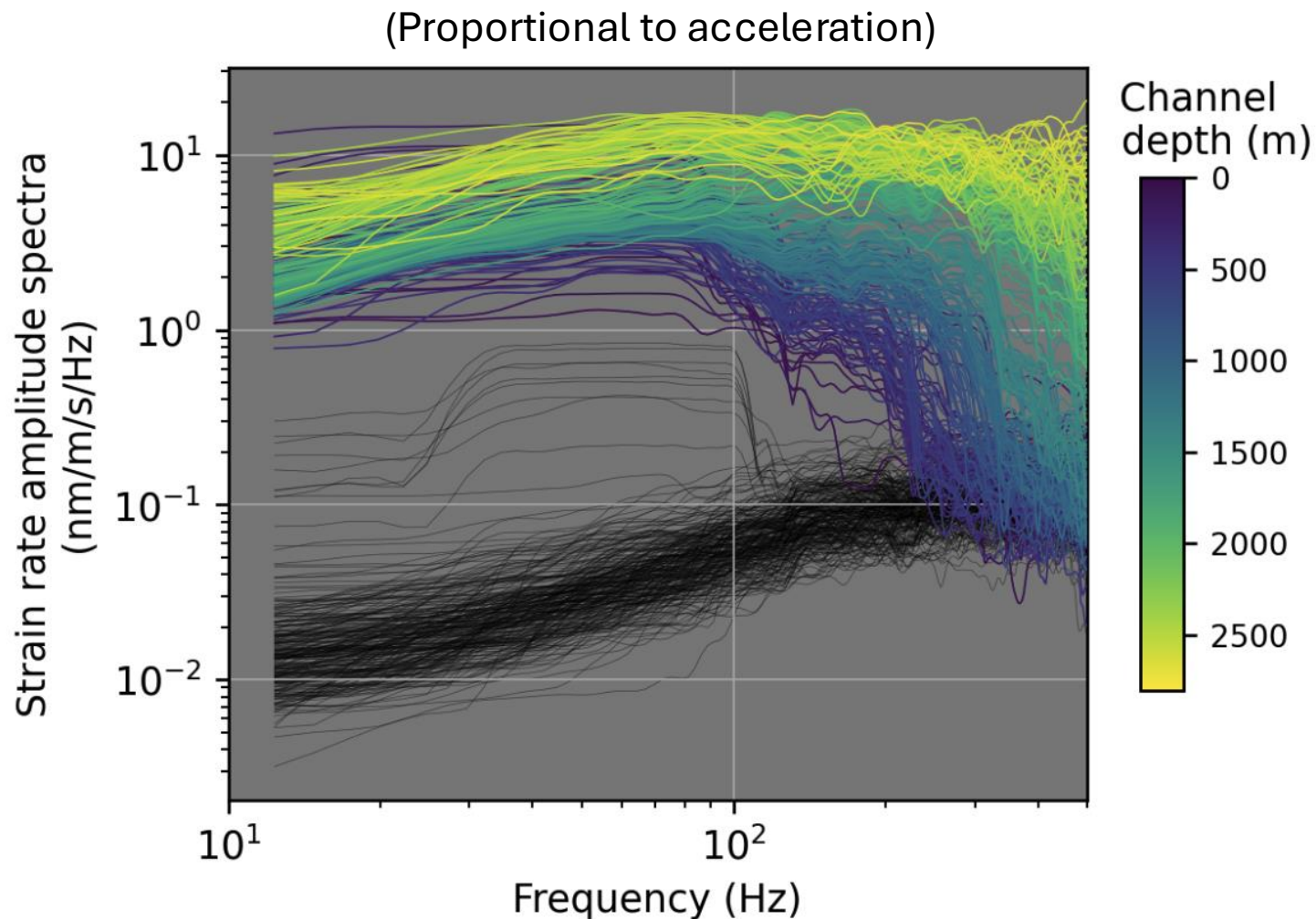
An event captured by the vertical cable



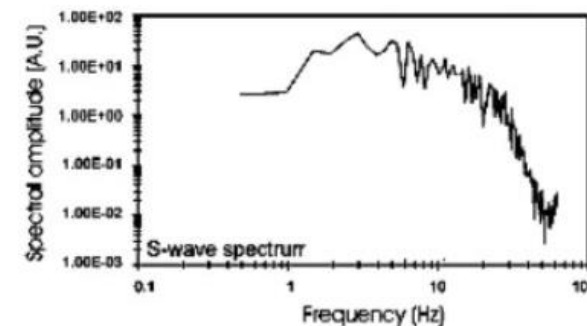
The workflow for source parameter estimation



Decomposing the P-wave spectra of DAS

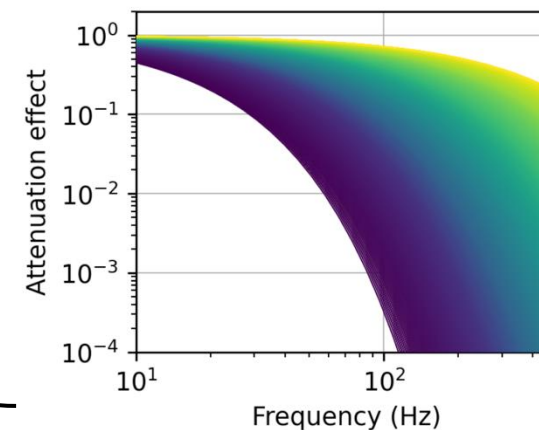


1. Source spectra



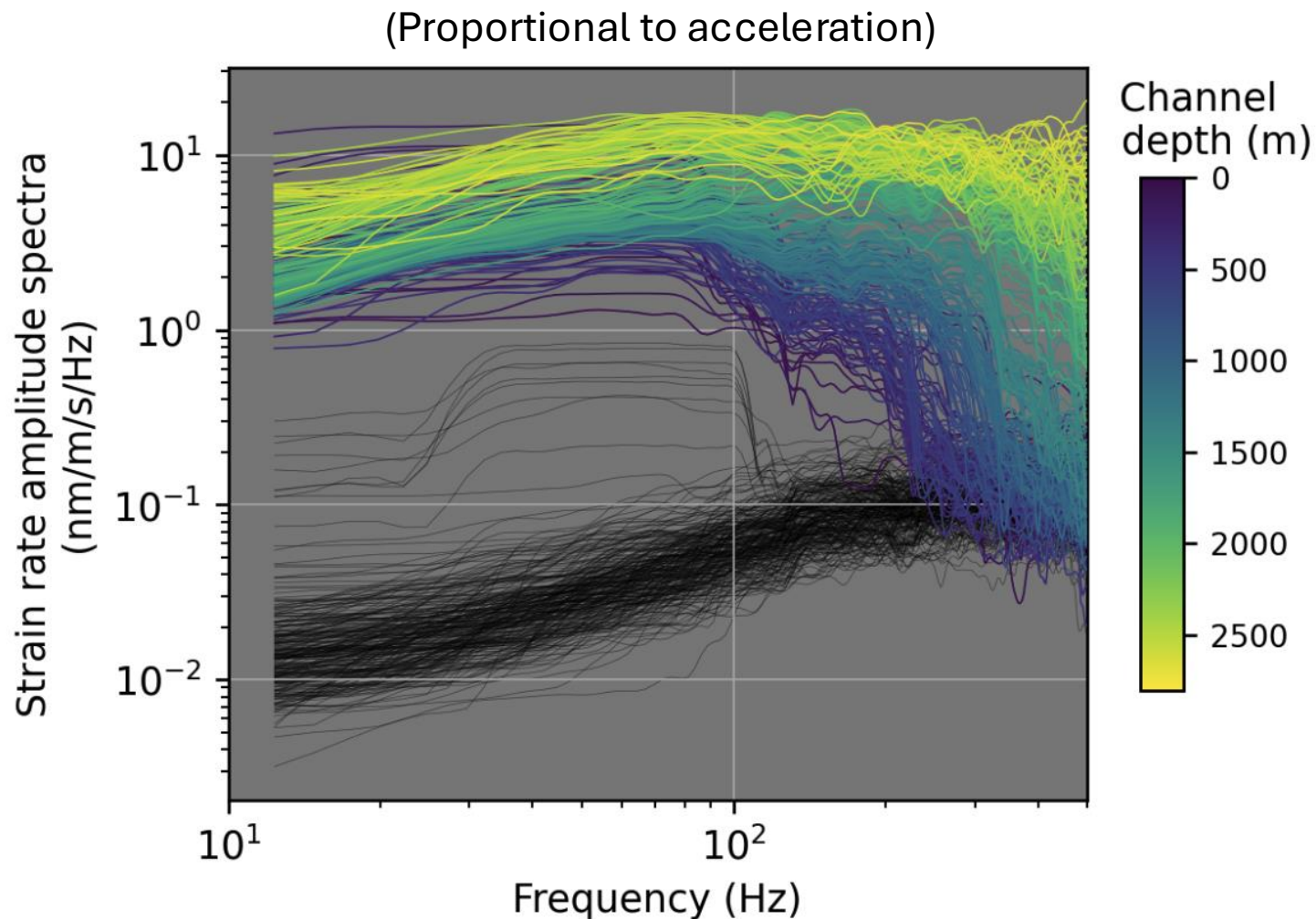
$$\frac{\Omega_0}{\left| 1 + \left(\frac{f}{f_c} \right)^{\gamma n} \right|^{\frac{1}{\gamma}}}$$

2. Attenuation

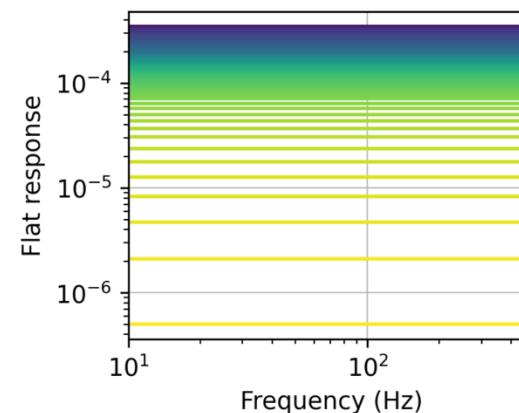


$$e^{-\pi f \kappa}$$

Decomposing the P-wave spectra of DAS



3. Sensitivity to incident angles



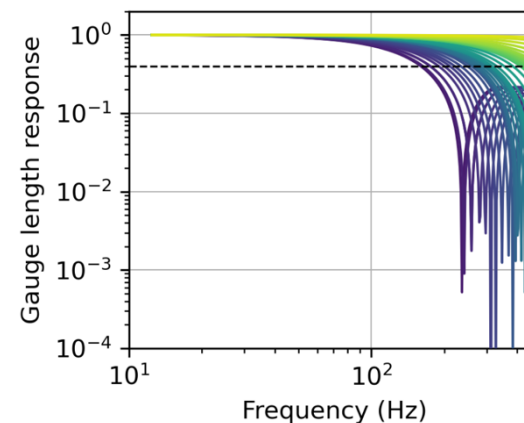
P waves

$$v \cdot \cos^2 \theta$$

S waves

$$v \cdot \cos \theta \sin \theta$$

4. Gauge length effect

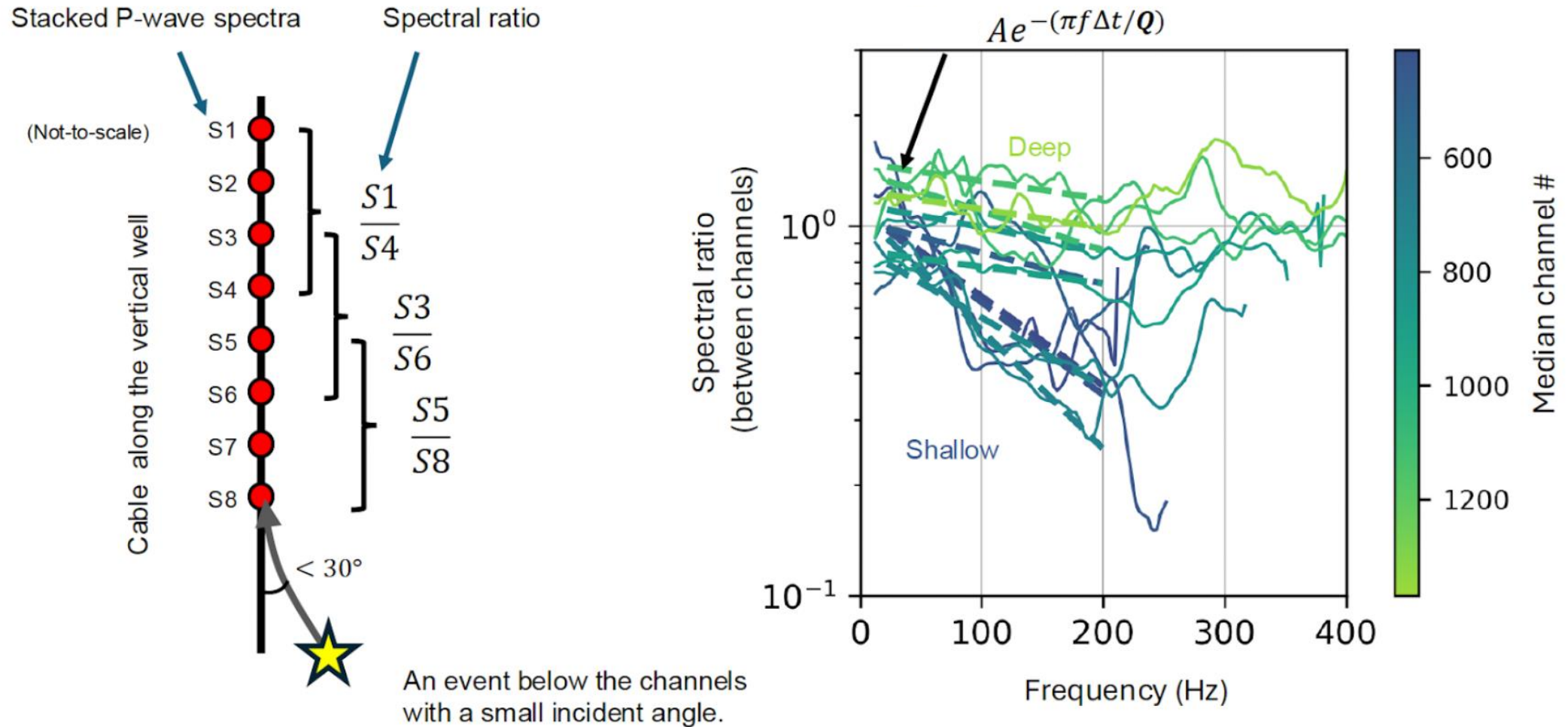


$$\text{sinc}\left(\frac{\pi f L}{v \cdot \cos \theta}\right)$$

L : Gauge length
(10 m)

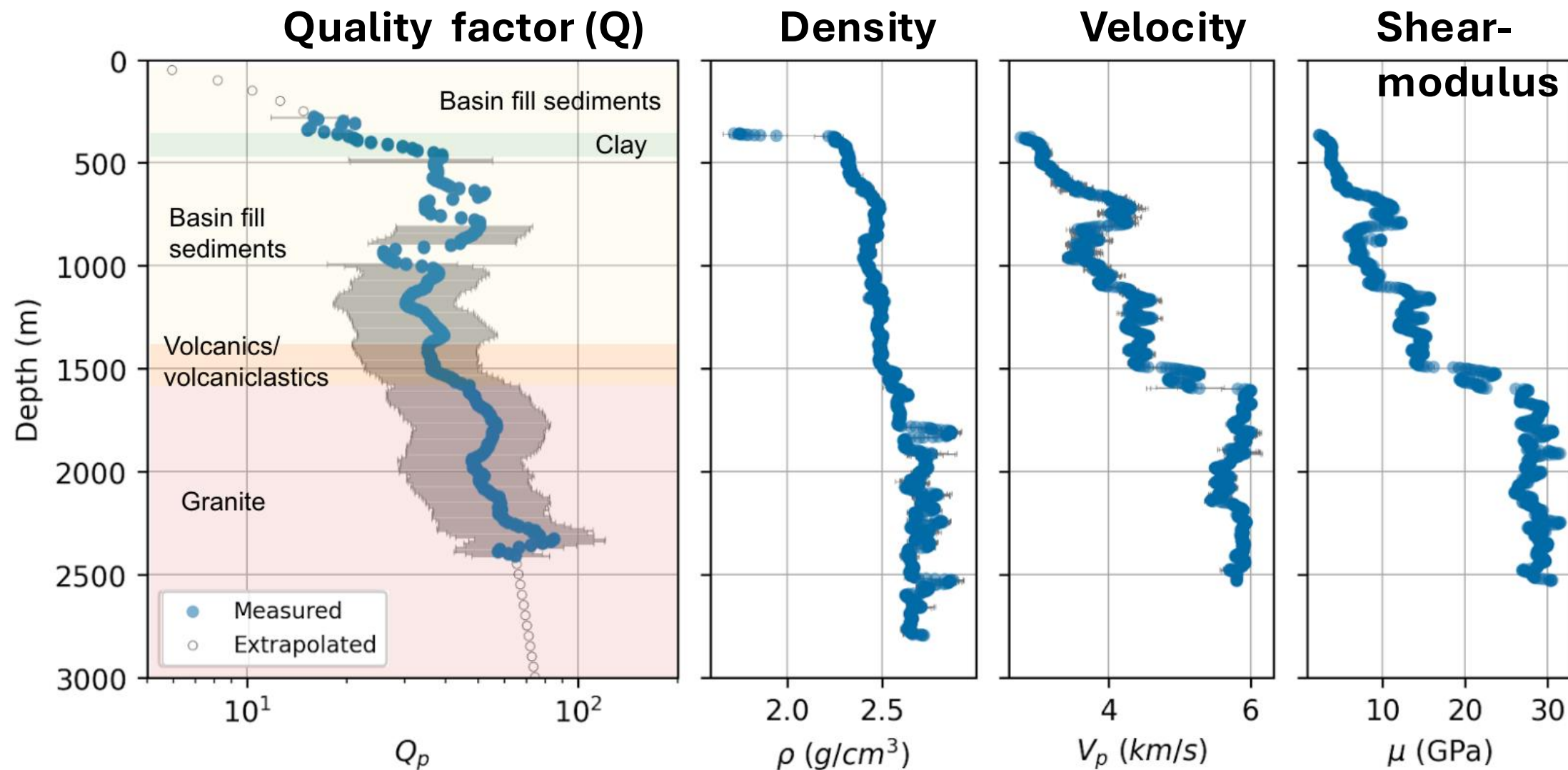
Bakku (2015)

Estimate attenuation using spectral ratio (along-depth)

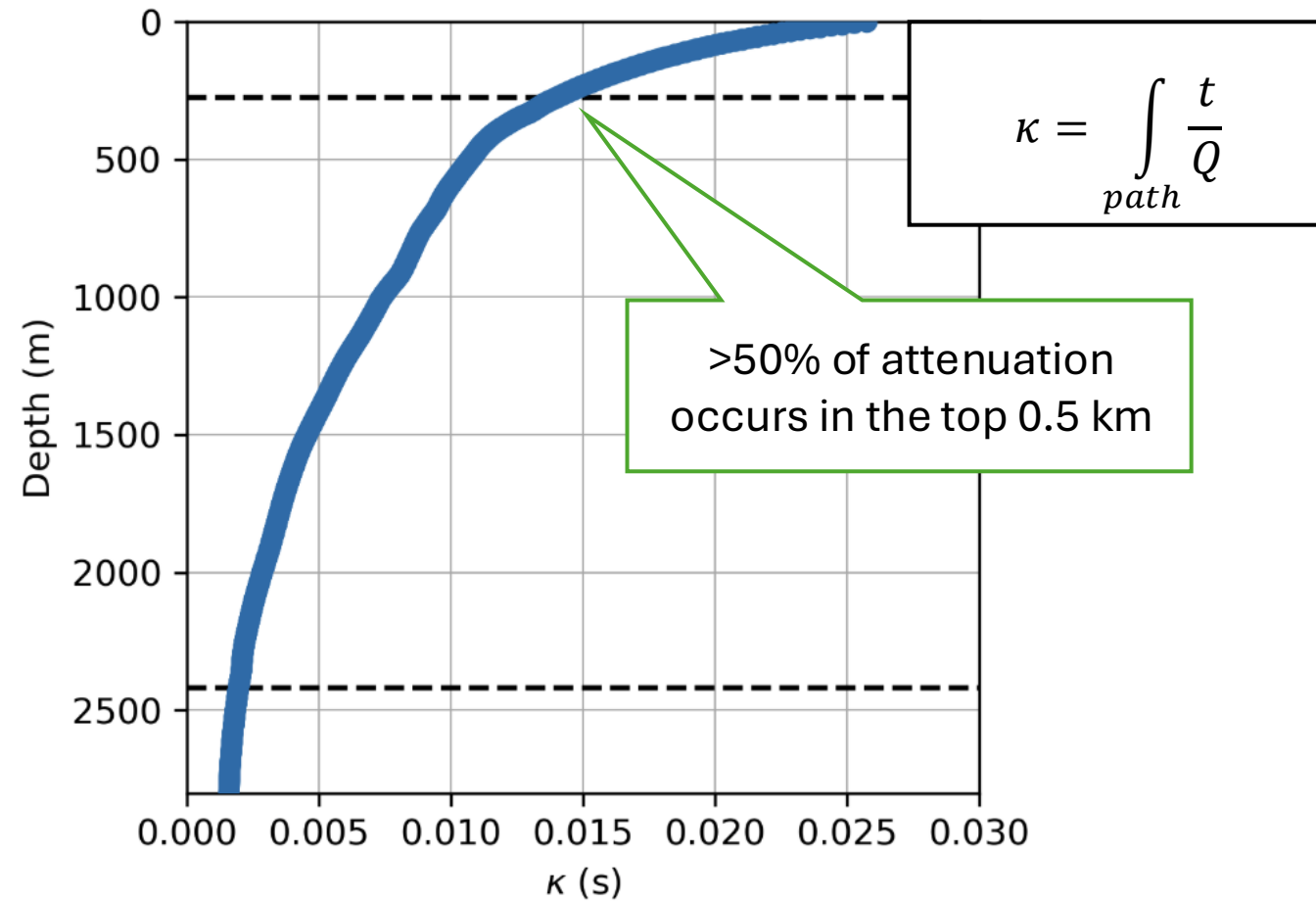
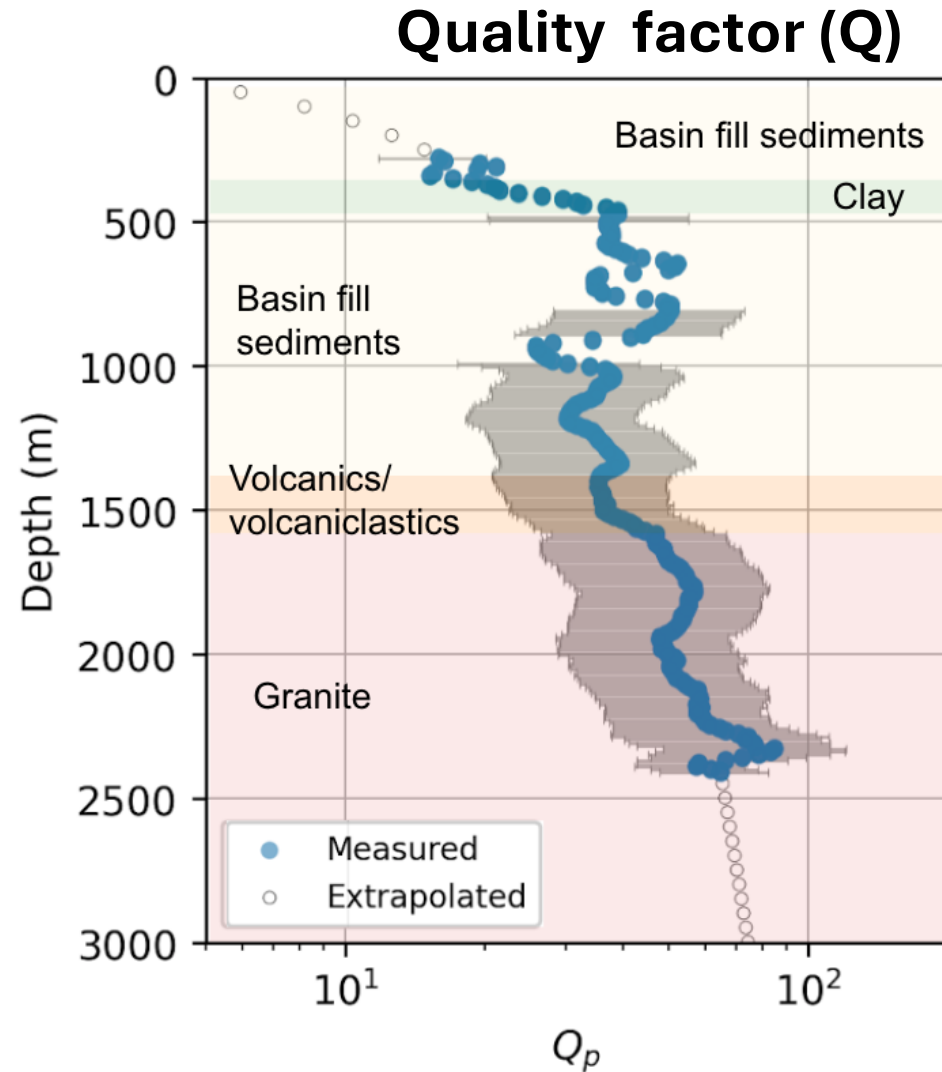


Q profile on the top 2.5 km

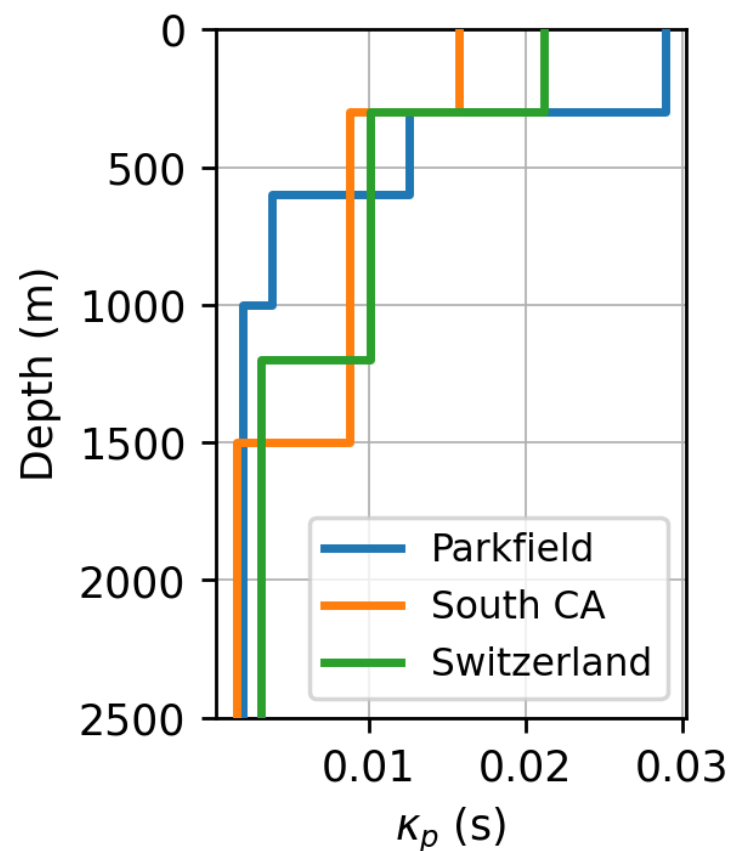
From well logs



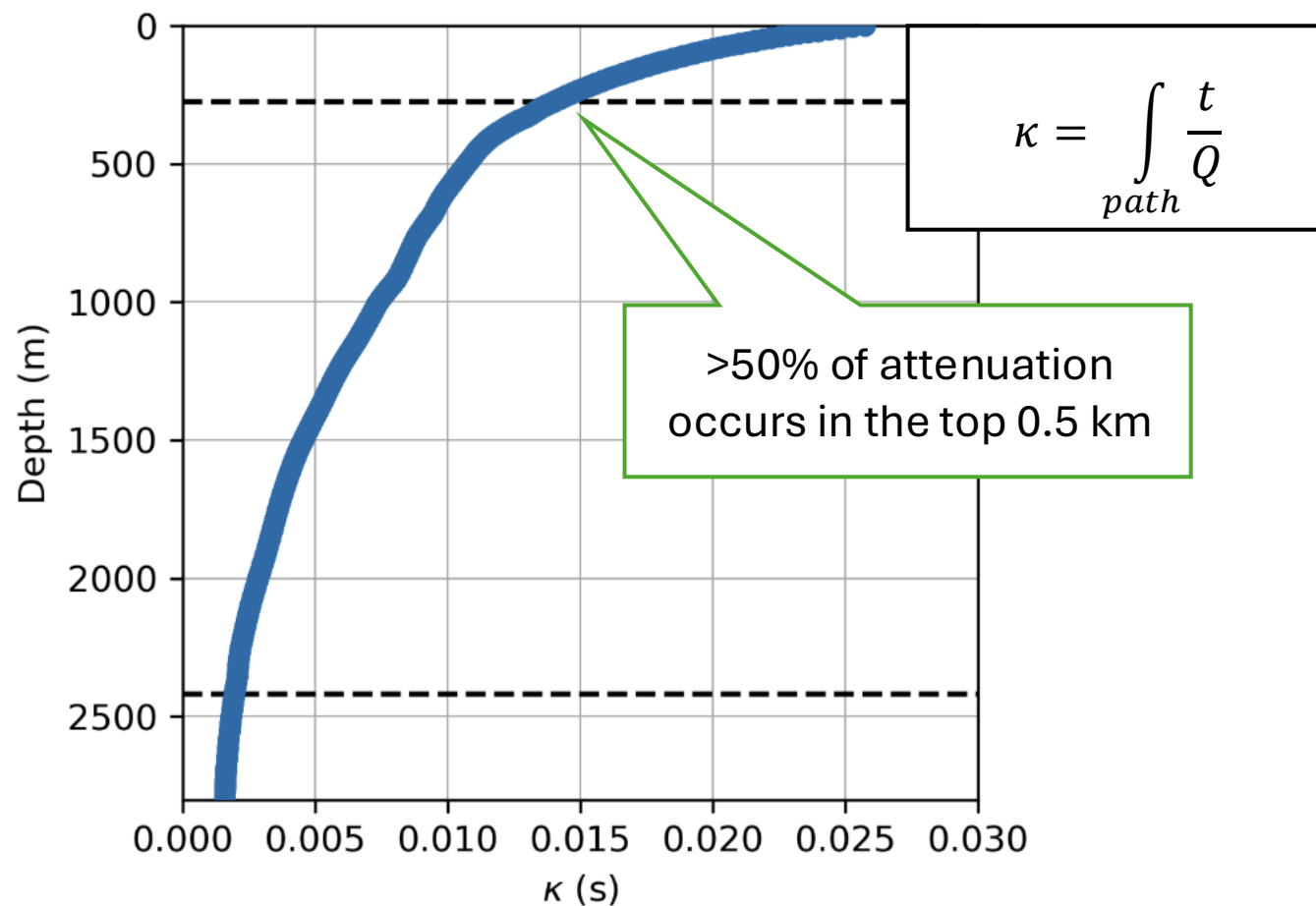
Accumulated attenuation (Kappa) for an event at the well bottom



Kappa agree with other attenuation studies

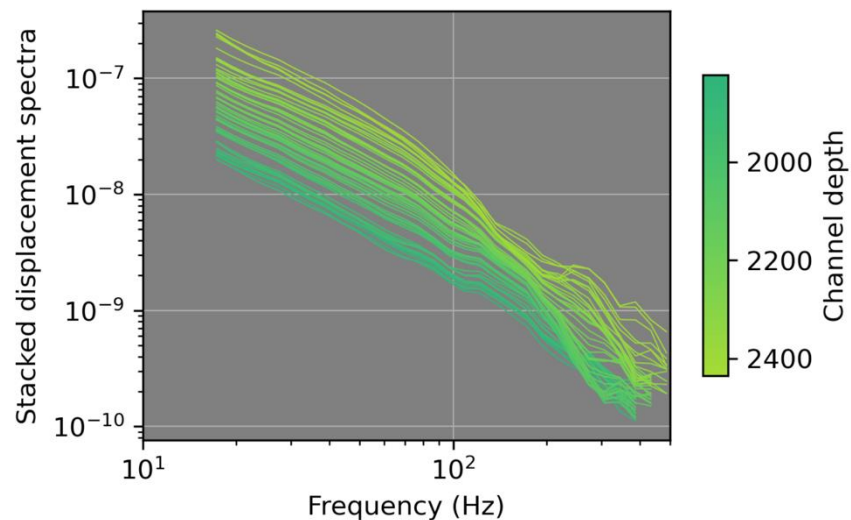


Jongmans & Malin (1995)
Abercrombie (1998)
Bethmann et al. (2012)



Single spectra fitting for source parameters

Stack channels every 20 m



Brune's model

$$\Omega_r = \frac{\Omega_0}{\left| 1 + \left(\frac{f}{f_c} \right)^{\gamma n} \right|^{\frac{1}{\gamma}}} \cdot e^{-\pi f \kappa}$$

$\gamma = 1$: Brune's model
 $n = 2$: High-f fall-off rate

$$\kappa = \int_{path} \frac{t}{Q}$$

Source radius

$$a = \frac{k\beta}{f_c}$$

β : Source Vs (from 1D model)
 $k=0.38$: (Kaneko and Shearer, 2014)

Seismic moment

$$M_0 = \frac{4\pi\rho c^3 R \Omega_0}{U_{\phi\theta}}$$

$\rho = 2790$: Density
 c : Source Vs (from 1D model)
 R : Hypocentral distance
 $U_{\phi\theta} = 0.52$: For P wave average radiation pattern (Madariaga, 1976)

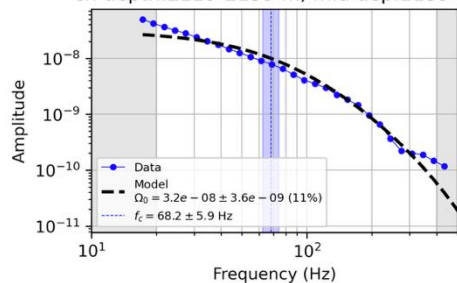
Spectral stress drop

$$\Delta\sigma = \frac{7}{16} \frac{M_0}{a^3}$$

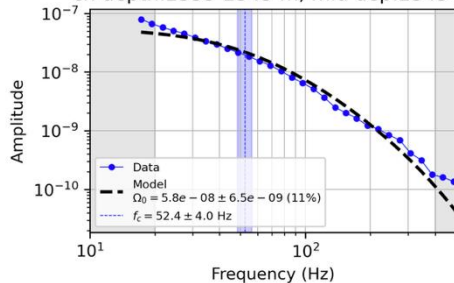
Quality Control

- Spectral point-wise SNR > 3
- $1.2 f_{min} < f_c < 0.8 f_{max}$
- Reduced chi-square (misfit) < 0.02
- Uncertainty < 50% (std/result)
- Incident angle < 45 deg
- Good cable (dep 2.0~2.4 km)

10B, iev: 65, M=1.53, stack_ch_num=10
 ch depth: 2129-2139 m, mid dep: 2139 m

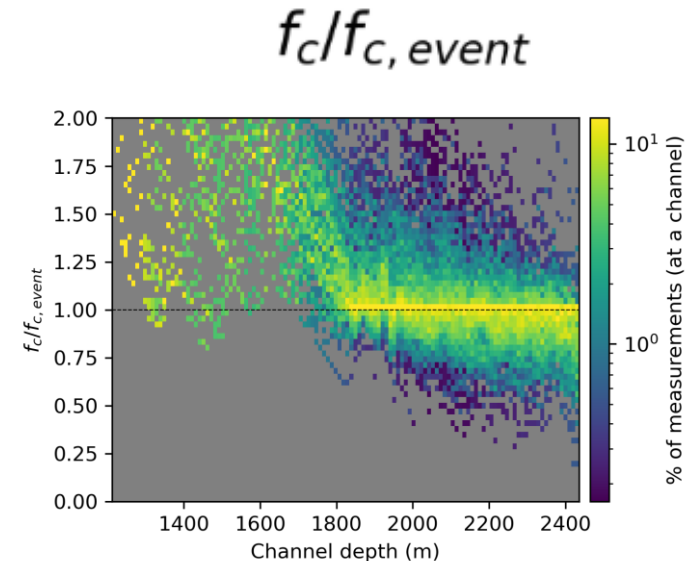
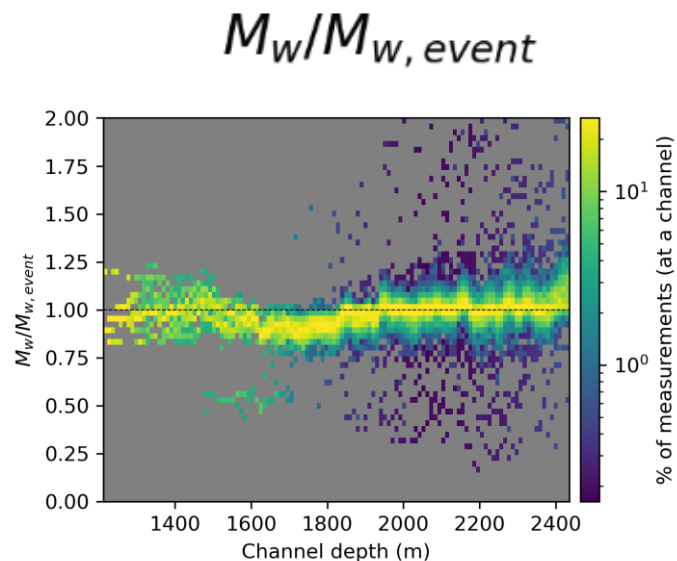
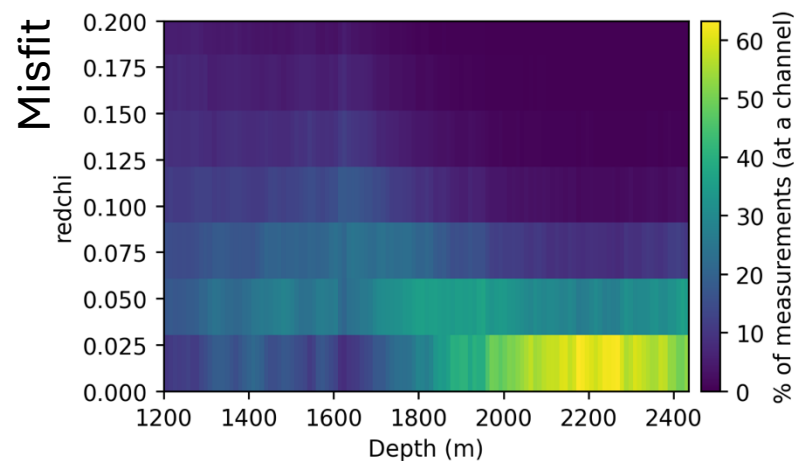


10B, iev: 65, M=1.53, stack_ch_num=10
 ch depth: 2333-2343 m, mid dep: 2343 m

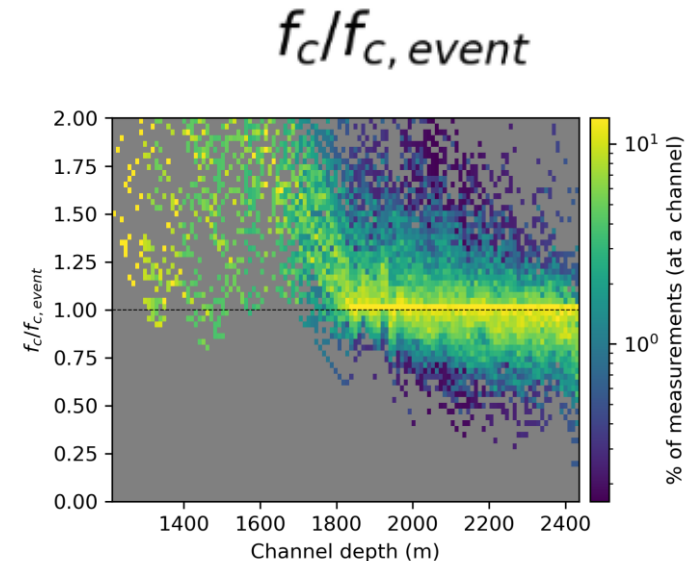
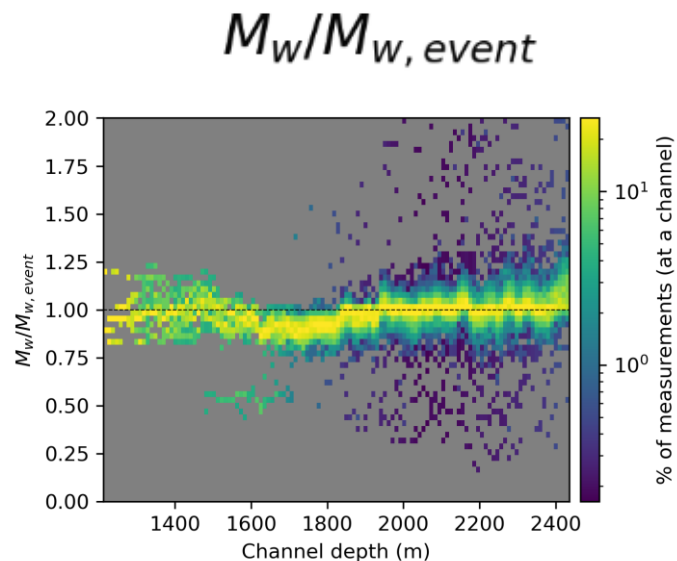
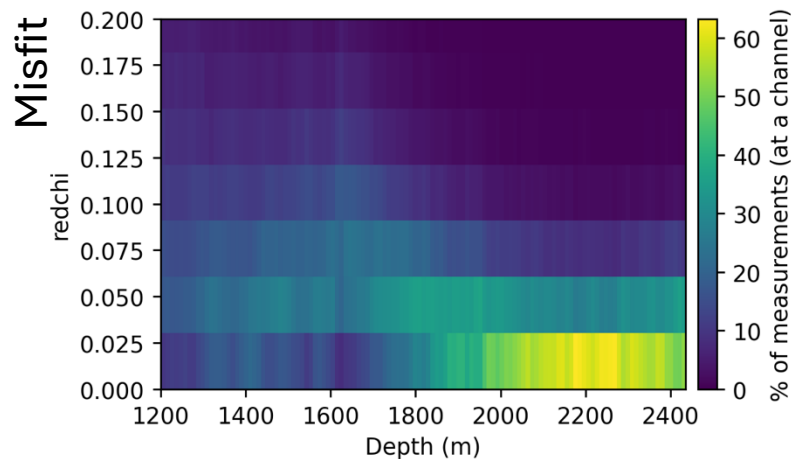


(Brune 1970; Madariaga 1976; Eshelby 1957)

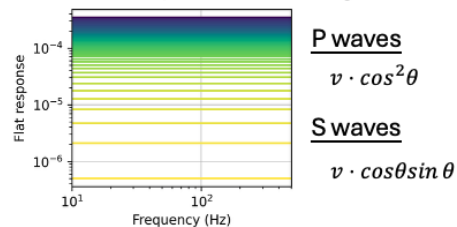
Which DAS channel to use matters



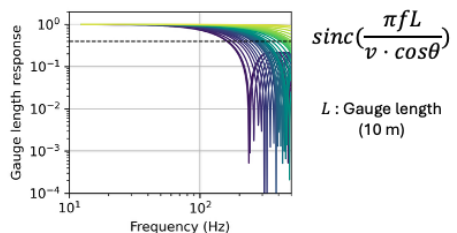
Which DAS channel to use matters



3. Sensitivity to incident angles



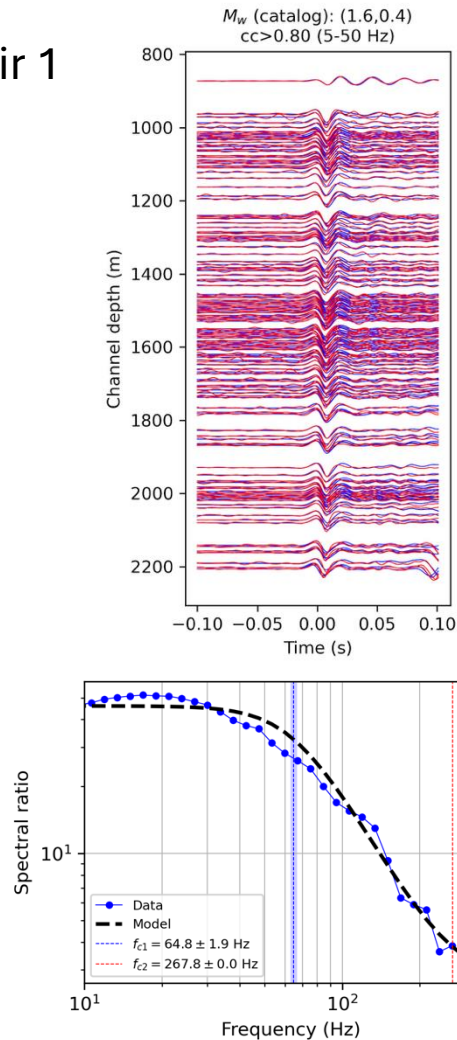
4. Gauge length effect



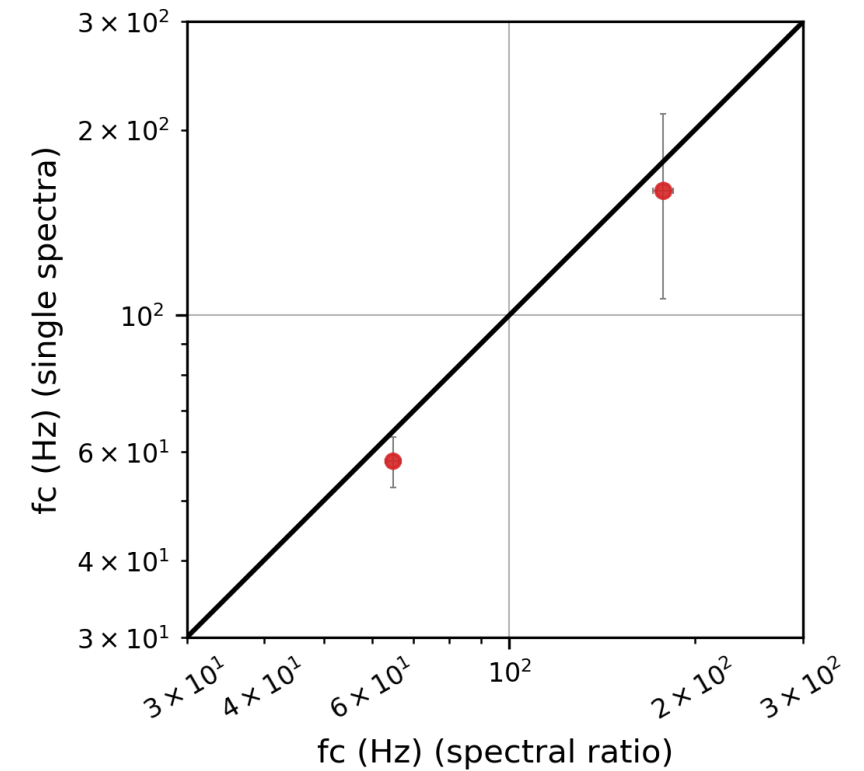
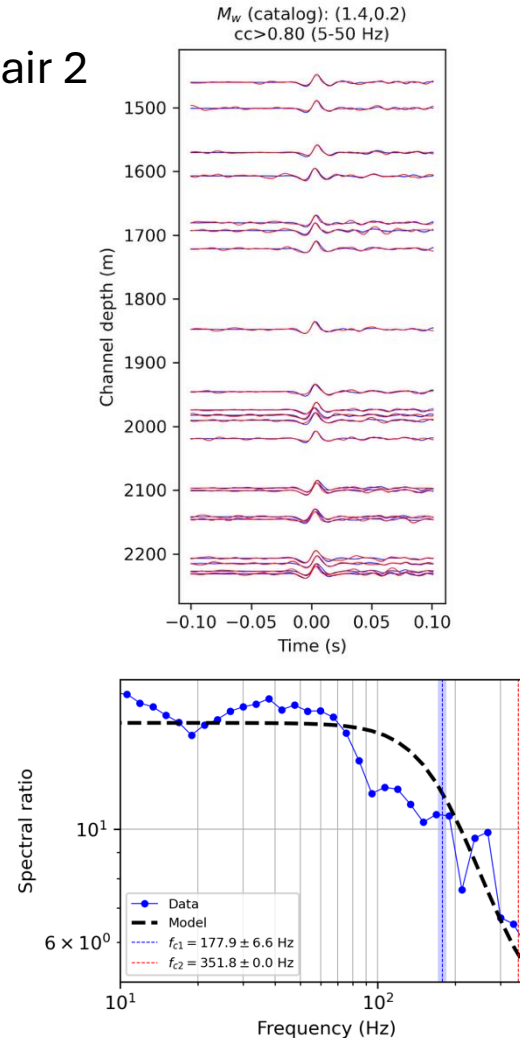
Uncertainty in incident angel can cause systematic bias in response removal
Possibly cause trade-offs with source parameters.

Compare f_c estimated using single spectra and the EGF approach

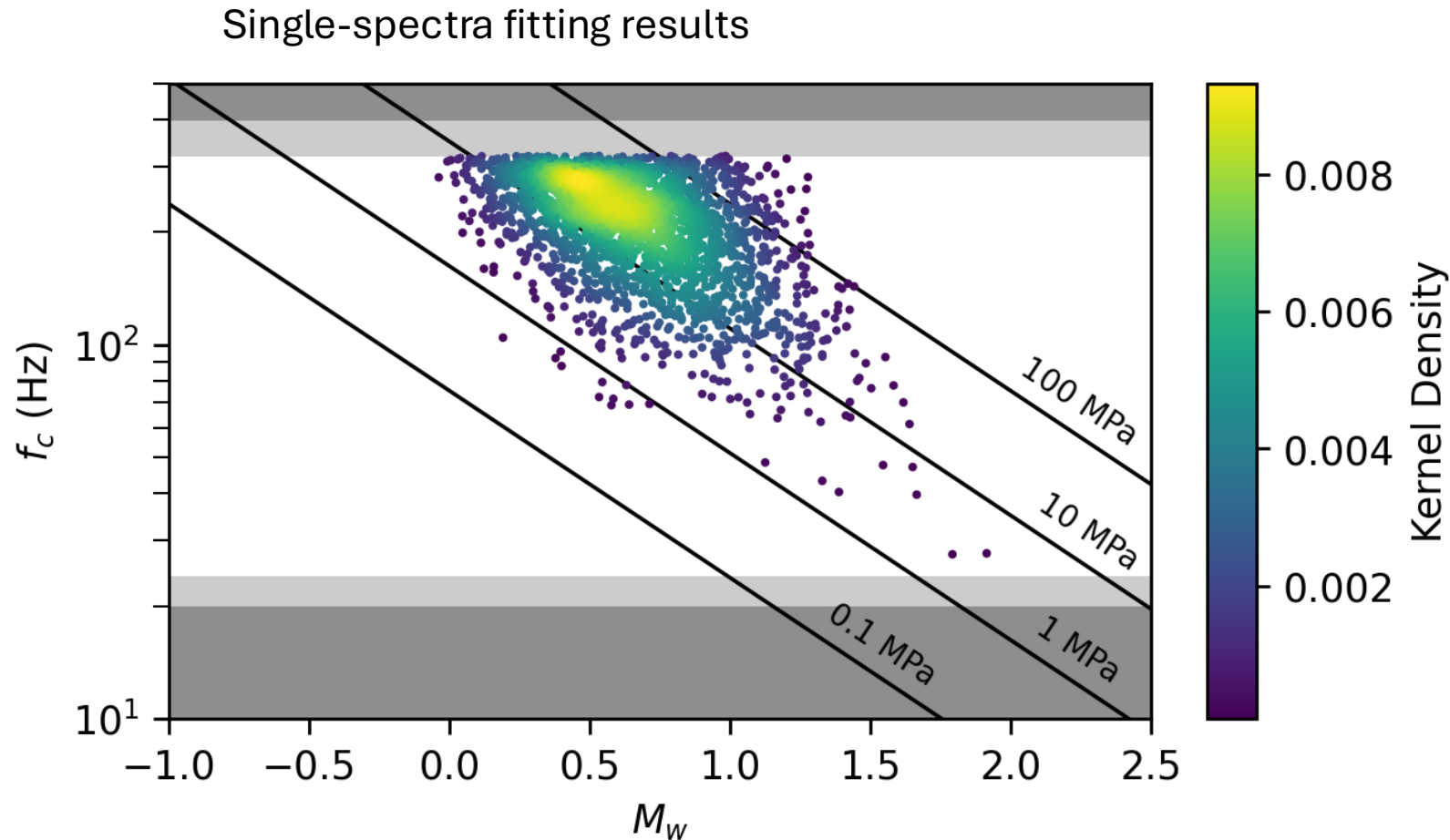
Event pair 1



Event pair 2

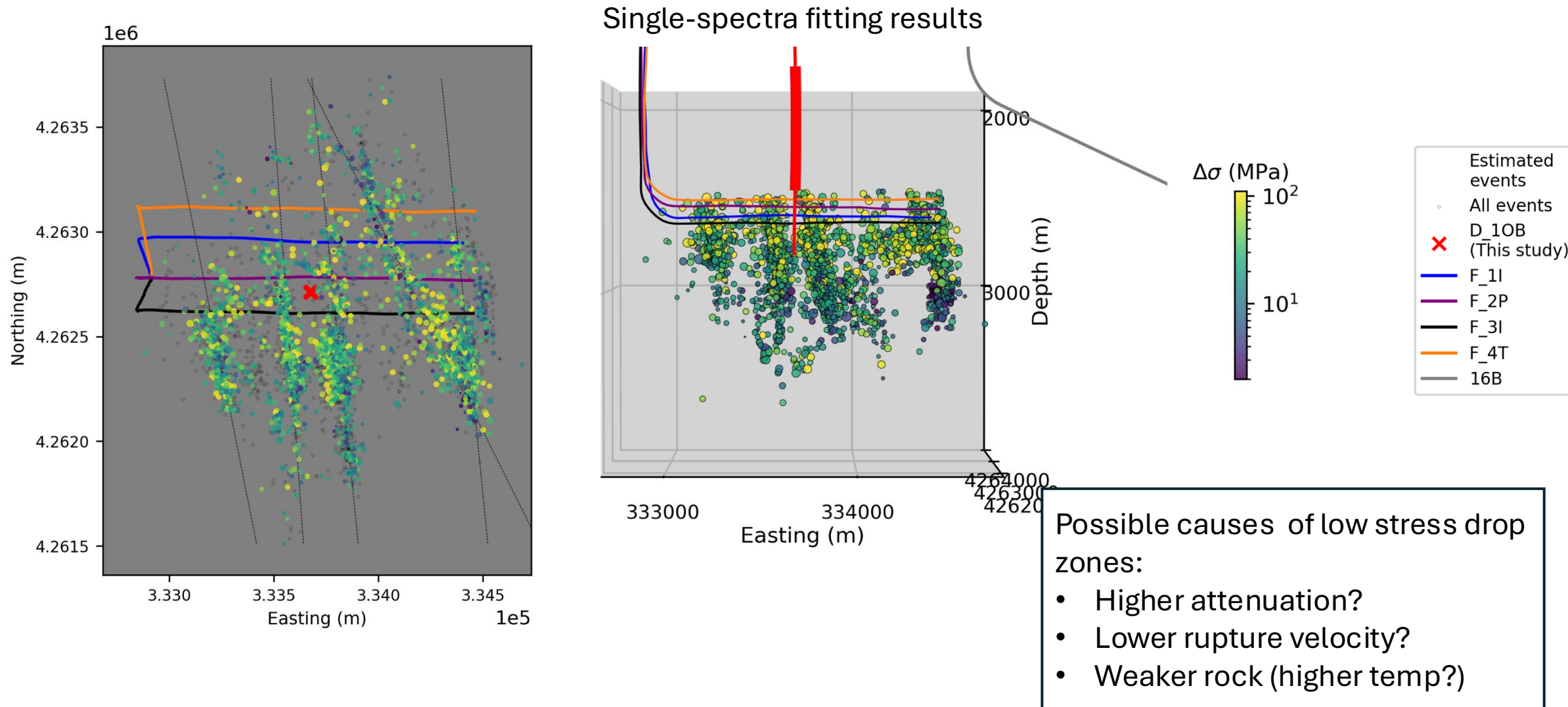


No evidence that the stress drop is magnitude dependent



- Median: 36.7 MPa
- A higher sampling rate (> 1000 Hz) is required to characterize smaller ($M_w < 0$) events.

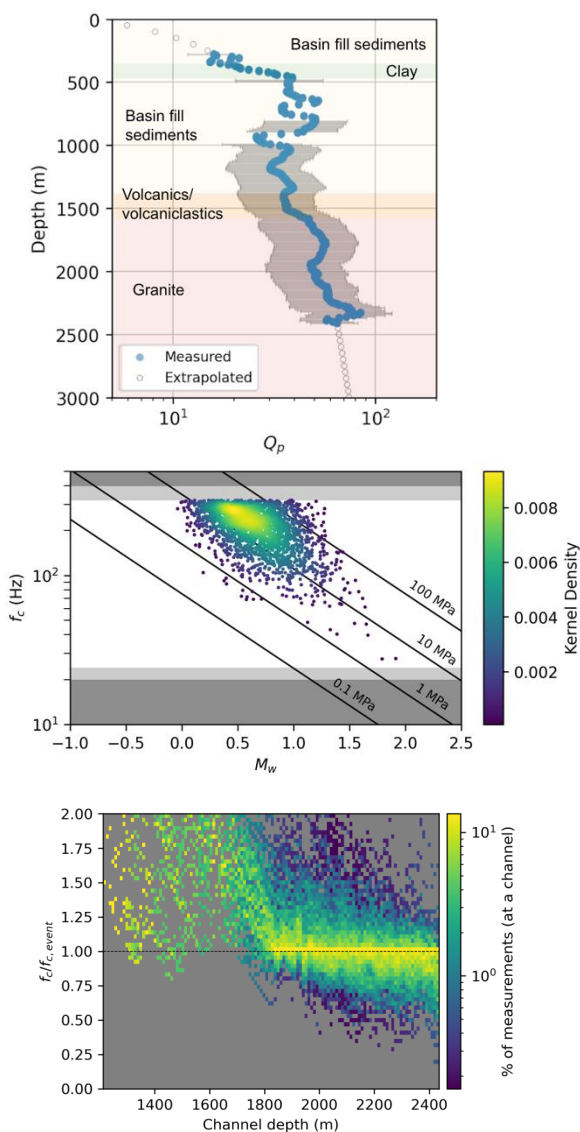
Mapping stress drops



Summary

- We estimate Q in the top 2.5 km in Utah.
 - Low Q in the top 0.5 km agrees with Parkfield, South CA (Cajon Pass), and Switzerland.
- We estimate spectral stress drop using single-spectra fitting for $0 < M_w < 2$.
 - No obvious deviation of constant stress drop
- DAS response removal can be another source of systematic bias.

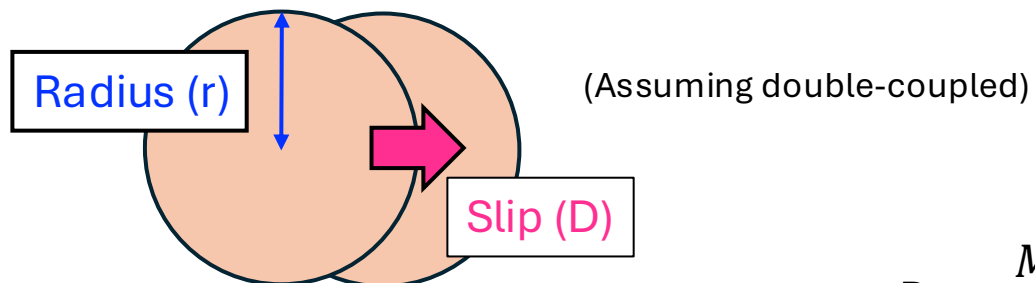
Chang, H., Nakata, N., Abercrombie, R. E., Dadi, S. & Titov, T. (in prep.). Characterizing shallow attenuation and microearthquake source parameters using downhole DAS array at the Cape Modem geothermal field.



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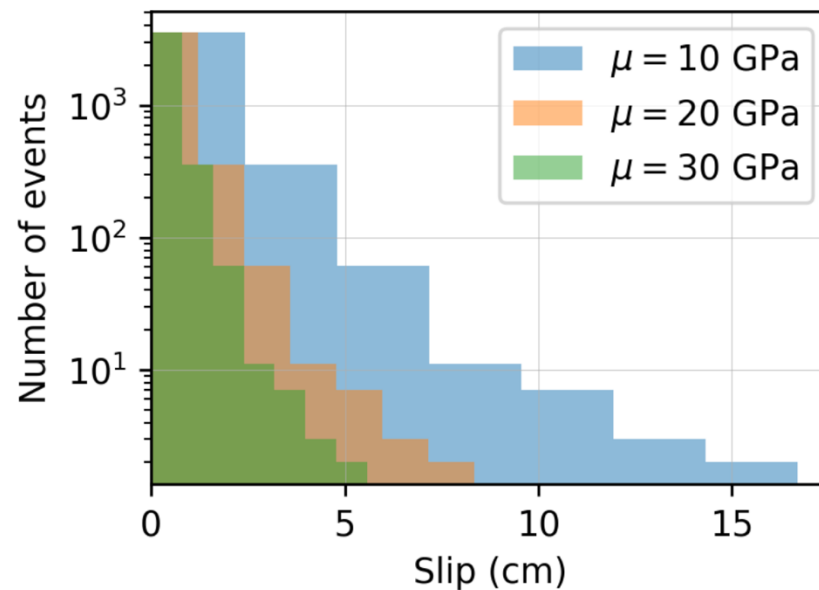
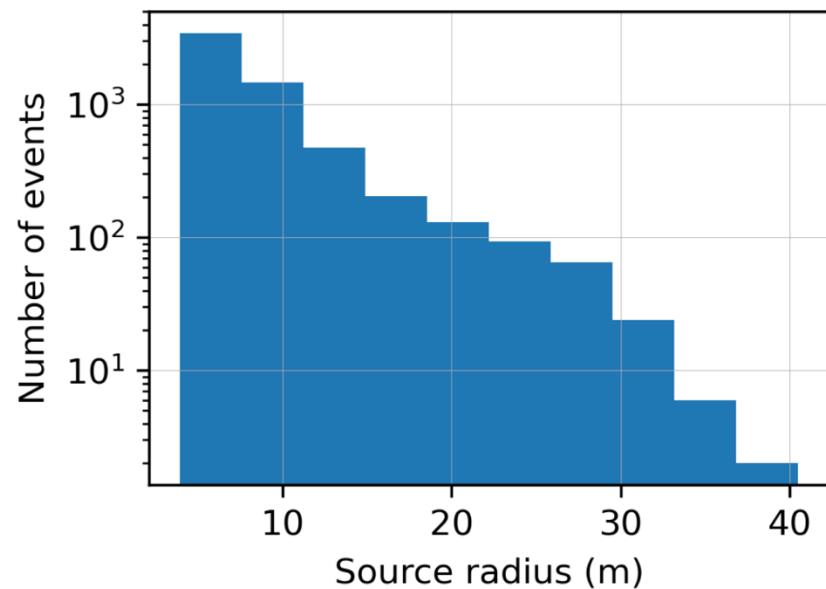
Source radius and slip



$$r = \frac{k\beta}{f_c}$$

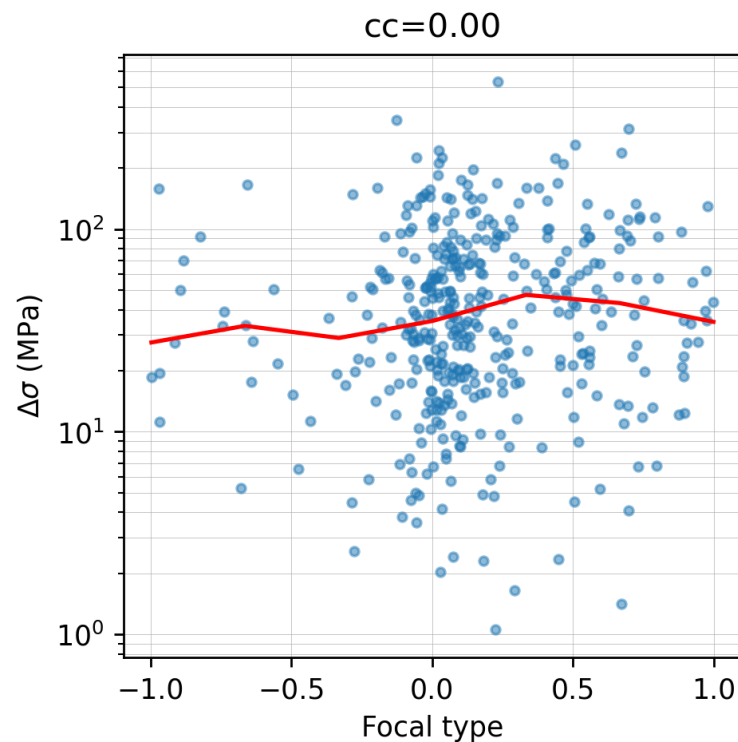
$k = 0.38$
 β : Shear-wave velocity

$$D = \frac{M_0}{\mu\pi r^2}$$



Assume different shear modulus (μ)

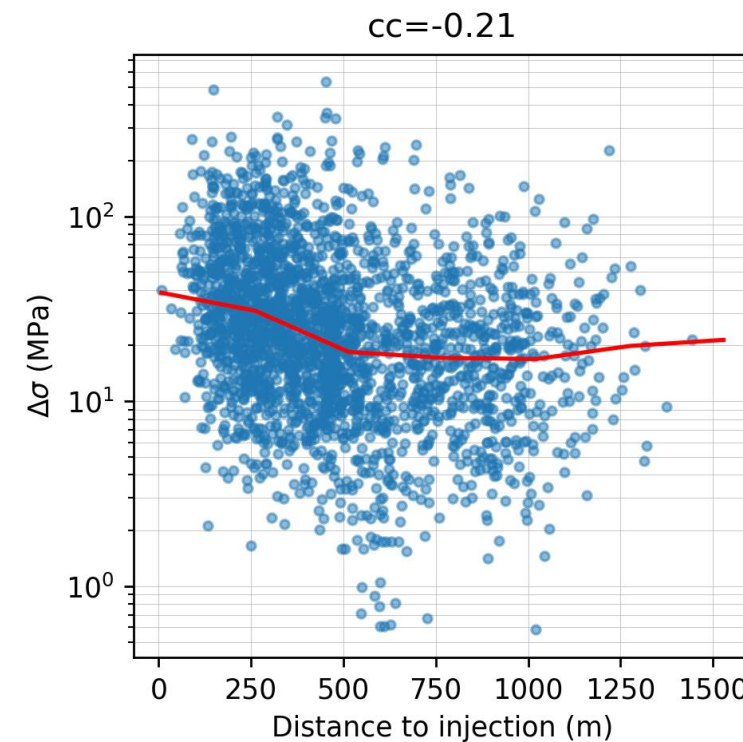
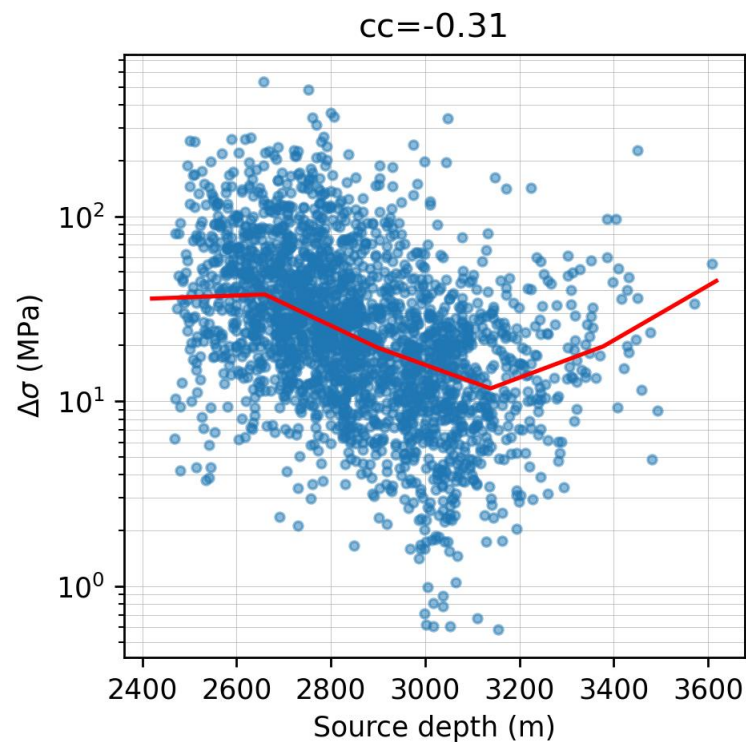
$\Delta\sigma$ vs focal mechanism, depth, injection distance



Normal

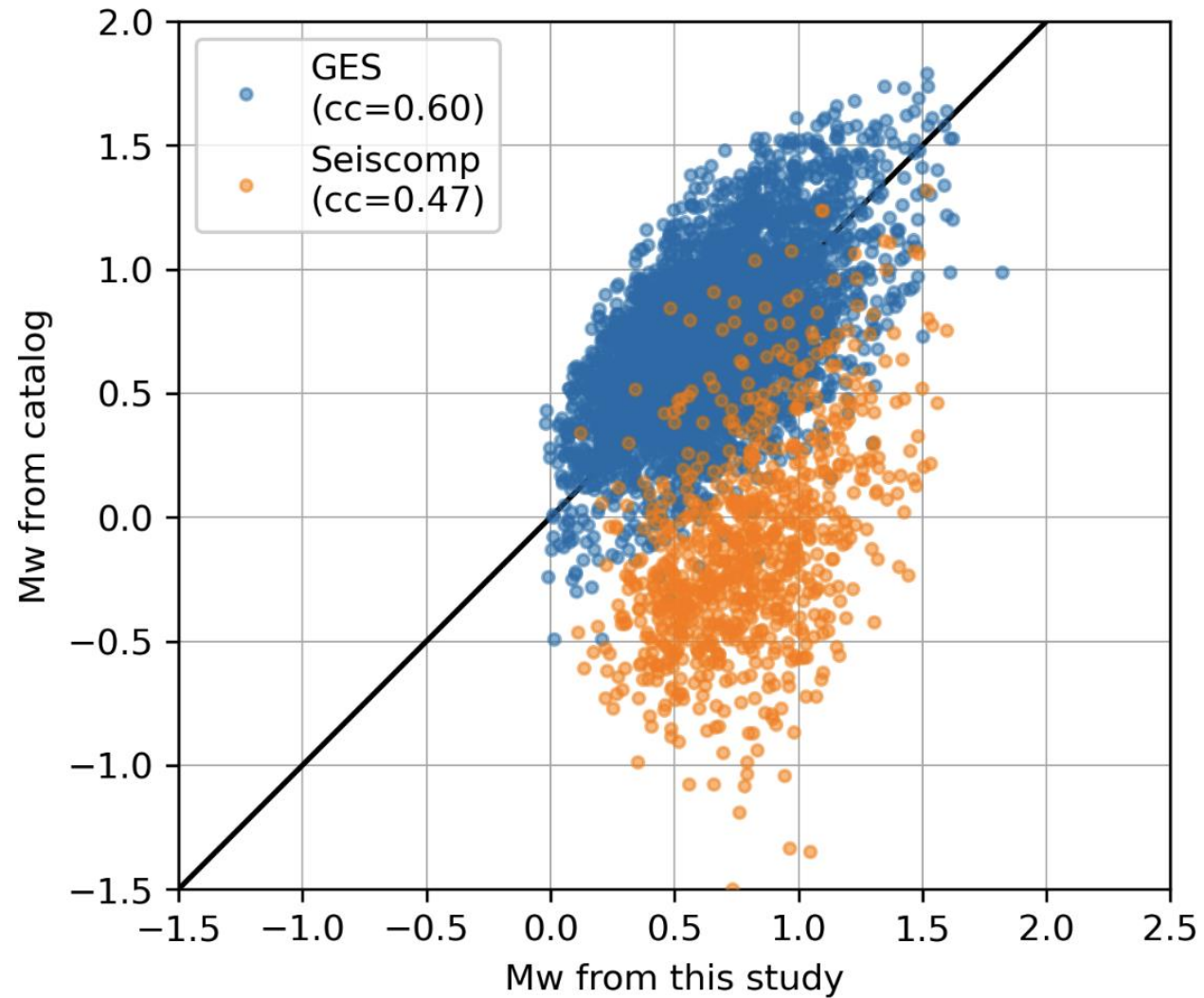
Strike-slip

Reverse

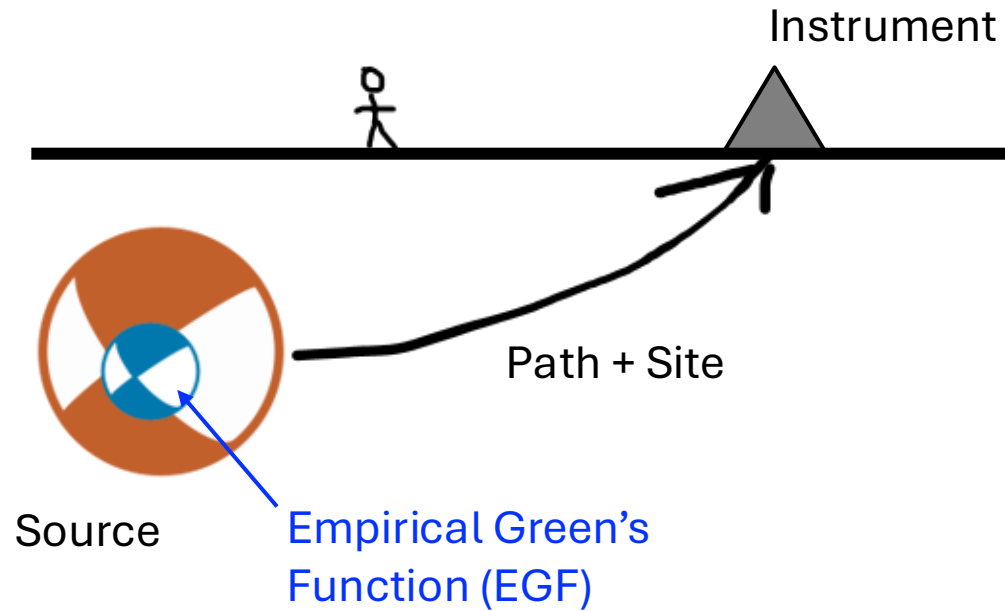


- Goertz-Allmann & Wiemer (2012) expected large distance, larger $\Delta\sigma$
- Opposite trend here because of $\Delta\sigma$ -depth correlation

Comparison with Mw estimated by surface network

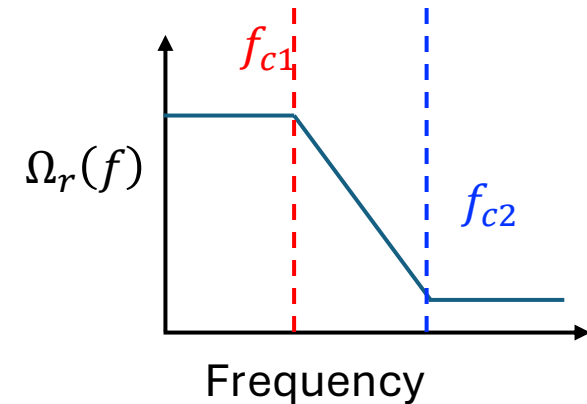


Spectral ratio (EGF) approach effectively avoids site-effect bias



$$\frac{U_1(f)}{U_2(f)} = \frac{\text{Source}_1(f) \cancel{\text{Path}(f)} \cancel{\text{Site}(f)} \cancel{\text{Instrument}(f)}}{\text{Source}_2(f) \cancel{\text{Path}(f)} \cancel{\text{Site}(f)} \cancel{\text{Instrument}(f)}}$$

$$\Omega_r(f) = \Omega_{0r} \left[\frac{1 + \left(\frac{f}{f_{c1}} \right)^{\gamma n}}{1 + \left(\frac{f}{f_{c2}} \right)^{\gamma n}} \right]^{1/\gamma}$$



However, an EGF can be difficult to find...

e.g., Need highly similar waveforms between target and EGF ($cc > 0.8$)